

I	Course Code	<b>MA197003</b>
II	Course Title	<b>Mathematical Theory of Finite Element Method</b>
III	Credits	L T P C 3 0 1 4
IV	Prerequisites (if any)	
V	Course Contents	<p><b>UNIT-I:</b> Elements of function spaces: Spaces of continuous functions, Spaces of integrable functions, Sobolev spaces; Weak solutions to elliptic problems, Lax Milgram Lemma: Existence and uniqueness of solutions. Piecewise Polynomial Spaces, Interpolation, L2-projection, Variational formulation of elliptic boundary value problems.</p> <p><b>UNIT-II:</b> Finite element methods: Galerkin orthogonality and Cea's lemma, Piecewise polynomial approximation in Sobolev spaces, Optimal error bounds in the energy norm, The Aubin-Nitsche duality argument, Numerical Integration, construction of element stiffness matrices and assembly into global stiffness matrix.</p> <p><b>UNIT-III:</b> Finite element approximation of Parabolic initial boundary value problems: Semidiscrete and fully-discrete schemes with convergence analysis.</p> <p><b>Lab Component:</b> Implementation of algorithms and computational experiments using MATLAB.</p>
VI	Text books/ References	<ol style="list-style-type: none"> <li>1. S. Brenner &amp; R. Scott, The Mathematical Theory of Finite Element Methods, Springer-Verlag, 1994.</li> <li>2. C. Johnson, Numerical Solution of Partial Differential Equations by the Finite Element Method. CUP, 1990.</li> <li>3. K.W. Morton, Lecture Notes on Finite Element Methods. Oxford University Computing Laboratory, 1991.</li> <li>4. M. G. Larson &amp; F. Bengzon, The Finite Element Method: Theory, Implementation and applications, Springer-Verlag, 2013.</li> </ol>